

8TH GRADE

NUMBER SYSTEMS EXPRESSIONS AND EQUATIONS FUNCTIONS GEOMETRY STATISTICS AND PROBABILITY





STUDENT INSTRUCTIONS

You will be completing a variety of problems and tasks within this math packet. The packet is broken down into the following topics:

- Number Systems
- Expressions and Equations
- Functions
- Geometry
- Statistics and Probability

Do your best within each section, and when finished, please fill out each section of the student reflection form.

STAY ON TRACK IN MATH!



NUMBER SYSTEMS

12.1														
ls the n	umbei	$r\frac{2}{3}$ ratio	onal or	irratior	nal?									
y?														
Is the n	umbei	r √22 r	ational	or irrat	tional?									
v?														
,														
Plot t	he foll	owing	numbe	rs on tł	ne num	ber line	e below	ı. Be sı	ire to la	abel ea	ch poir	nt with i	its letter:	
π	(b)	2.666	566666			(c) −√1	6	(d)	√36	(6	e) $\frac{1}{4}$	(f)	$-\frac{2}{3}$	
	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	
이ot the	numb	er $\sqrt{17}$	on th	e numb	oer line	below.	Explai	in belov	w how	you are	e able t	o appro	oximate the	
nber to	the te	nths pl	ace wit	hout u	sing a c	alculate	or.							
	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	
Explain:														
Explain:														
Explain:														
Explain:														
Explain: ^{8.NS.1} 5. Wha	at is th	e diffe	rence b	etweer	n a ratio	onal an	d irratio	onal nu	mber?					
Explain: ^{8.NS.1} 5. Wha Explain	at is th below	e diffei	rence b	etweer	n a ratio	onal an	d irratio	onal nu	mber?					
Explain: ^{8.NS.1} 5. Wha Explain	at is th below	e diffei :	rence b	etweer	n a ratio	onal an	d irratio	onal nu	mber?					
Explain: ^{8.NS.1} 5. Wha Explain	at is th below	e diffei :	rence b	etweer	n a ratio	onal an	d irratio	onal nu	mber?					
Explain: 8.NS.1 5. Wha Explain 6. State	at is th below	e diffei : her ead	rence b	etweer ber is e	n a ratio	onal and	d irratio	onal nu ional:	mber?					
Explain: 8.NS.1 5. What Explain 6. State (a) –23	at is th below	e diffei : her ead	rence b	etweer ber is e	n a ratio	onal and ational	d irration or irrat	onal nu ional:	mber?					

Now that you are finished with this section, fill out the **NUMBER SYSTEM** section of the **REFLECTION FORM**.

EXPRESSIONS AND EQUATIONS

8.EE.1
1. Simplify each expression. Be sure your answers have positive exponents:
(a) $3a^6 \cdot 6a^4 =$ (b) $\frac{20b^{12}}{5b^3} =$ (c) $(x^4)^6 =$
(d) Write 2 possible answers for this problem: $4^3 \cdot 4^{-6} =$ or
8.EE.2
2. Solve each problem involving square or cube roots:
(a) What is the cube root of 27? (b) What is the square root of 121?
(c) Solve the equation: $x^2 + 3 = 67$
Solution(s):
(d) A square has an area of 324 m^2 . What is the measure of one side? meters
8.EE.3, 4
3. Solve each problem involving scientific notation:
(a) Write .0000306 in scientific notation:
(b) Write 7,900,000,000 in scientific notation:
(c) A CEO's salary is \$5,000,000 per year. A first-year teacher's salary is \$25,000. How many times larger is the CEO's salary? Keep your numbers in scientific notation as you set up and work out the problem. Show steps below:
The CEO's salary istimes larger.
(d) Is this number in scientific notation? 13×10^8 . (Yes or No.)
How do you know?
If you answered "no," make the corrections:
(d) Multiply: $(4.6 \times 10^8) \bullet (3.8 \times 10^6) =$

EXPRESSIONS AND EQUATIONS

4. The table shows the change in altitude of a hiker. What is the hiker's rate of change?

Minutes	Altitude (ft)
0	0
3	150
4	200
5	250
6	300

The hiker's rate of change is _____.

8.EE.6

5. Draw a "slope triangle" on the graph to find the slope of the line. (Remember...slope is $\frac{rise}{run}$.)



Slope of the line =

Now, try it again, but create a new slope triangle that is a different size. Do you get the same answer for the slope?

Why did that happen? Explain:

6. Write an equation for each line. Be sure your equation is in the form y = mx + b.



(a) Equation: _____



(b) Equation: _____







(c) Equation: _____

8.EE.5

8.EE.7

EXPRESSIONS AND EQUATIONS



11. Determine if (-4, 6) is a solution for this system of equations:

Is the ordered pair a solution? ______ Explain how you know:

Now that you are finished with this section, fill out the **EXPRESSIONS AND EQUATIONS** section of the **REFLECTION FORM**.

8.F.1

1. Tell whether or not each situation represents a function.

(a) Ordered Pair: (3, 5), (6, 8), (7, 5), (8, 10) Function? (Yes or no.)

Explain: _____

(b) Table:	х	У	
	5	8	Function? (Yes or no.)
	10	7	Explain:
	6	4	
	5	3	
	4	10	
(c) Graph:			Function? (Yes or no.) Explain:
÷		/	

8.F.2

2. Tell which function has a greater rate of change...the graph or the table:



y
76
60
44
28
12

Which has the greater rate of change?

Rate of change: _____



3. Graph each equation. Then tell whether or not your graph represents a function.



8.F.4

4. Write an equation in function form for each linear relationship below:





8.F.5
5. The graph at the right tells a story. In your own words, describe what is happening to the y-values as the x-values are increasing from 0 to 10. Be sure to use words like increase, decrease, constant, linear, or nonlinear.





8.F.5

6. Sketch a graph that could exhibit the qualities in the description below:

Between the x values of 0 and 4, the y values increase in a nonlinear pattern. Then, the y values stay constant between the x values of 4 and 6. Then, from x values of 6 to 10, the y values decrease in a linear pattern.



Now that you are finished with this section, fill out the **FUNCTIONS** section of the **REFLECTION FORM**.



8.G.1

1. Triangle ABC has coordinates A(-8, 6), B(-4, 5), C(-6, 3). Complete the series of transformations below. Graph each new image and give the new image coordinates:



Are both line segments congruent? Yes or No: _____

L	
3.	Give the rule in coordinate notation for a reflection over the x-axis:
4.	Give the coordinate rule for a reflection over the y-axis:
5.	Give the coordinate rule for a 180° rotation about the origin:
6.	Give the coordinate rule for a 90° clockwise rotation about the origin:
7.	Give the coordinate rule for a 90° counterclockwise rotation about the origin:
8.	Give the coordinate rule for a dilation of a figure using a scale factor of 3:
W	hich type of dilation does your rule represent? (Enlargement or Reduction):

9. A triangle is translated 8 units to the left and 2 units up in the coordinate plane. Describe the rule in coordinate notation:

8.G.4

863

10. Dilate triangle ABC using the rule $(x, y) \rightarrow (\frac{1}{3}x, \frac{1}{3}y)$. Be sure to label the vertices of your image.



11. Which type of transformations will result in a congruent image?

12. Explain what it means for 2 figures to be congruent:

13. Use the diagram below to find the missing angle measures.



14. Use the diagram below to answer the fill in the blanks. Lines a and b are parallel:



- (a) $\angle 7$ and _____ are corresponding angles.
- (b) $\angle 2$ and _____ are alternate interior angles.
- (c) $\angle 4$ and _____ are alternate exterior angles.
- (d) $\angle 6$ and _____ are vertical angles.
- (e) ∠3 and _____ are consecutive interior angles.
- (f) If $m \ge 1 = 132^\circ$, then $m \ge 7 = _$.

15. $\triangle ABC$ and $\triangle DEF$ are similar. If $m \angle B = 62^\circ$, then $m \angle E =$



8.G.5

8.G.6

17. Explain how you know this is a right triangle:

17 units 8 units 15 units

8.G.7

18. A ladder is leaning against a brick wall. The bottom of the ladder is 5 feet from the wall. The top of the ladder reaches the wall 12 feet up from the ground. **How long is the ladder?**

Steps and Solution:



Steps and Solution:



8.G.8

20. Use the Pythagorean Theorem to find the distance between points A and B in the coordinate plane. Round your answer to the nearest hundredths place.

Steps and Solution:





21. Find the volume of the cone, cylinder and sphere below. Use 3.14 for π . Round all answers to the nearest whole number:



22. For the back-to-school open house, the middle school put a huge blow-up pencil in the front of the building! Find the volume of the pencil. Use 3.14 for π and round your final answer to the whole number.



Show Steps and Solution:

STATISTICS AND PROBABILITY



8.SP.1

1. Which scatterplot below *best* illustrates the relationship between hours studying and test scores earned? *Circle your choice:*







Explain how you decided:

2. Create a scatterplot below that shows these characteristics: Negative Correlation

One outlier

What might your scatterplot depict? Give a real-world example of a situation your graph could represent:

8.SP.2

3. Draw a line of fit for the scatterplot below:



STATISTICS AND PROBABILITY

Step 1: Find the y-intercept:

8.SP.3

4. Use the step-by-step approach at the right to write an equation for the line of fit.



5. Find 8 friends or family members and measure their height, foot length, and hair length. Fill in each table below with the data. Afterward, answer the questions at the right:

Height (cm)	Foot Length (cm)	Height (cm)	Hair Length (cm)	 (a) What association(s), if any, do you see for the Height/Foot
				(b) What association(s), if any, do
				you see for the Height/Hair Length table?

Now that you are finished with this section, fill out the **STATISTICS AND PROBABILITY** section of the **REFLECTION FORM**.

NI -		
בוא	mo	
iva	IIIC.	

STUDENT REFLECTION FORM

Directions: After completing each section of the packet, fill out this sheet in the corresponding section. Please be honest! This will let your math teacher know how you have progressed. Maybe you've mastered certain topics, or perhaps you need additional help in others. Your teacher is there to provide help if needed!

NUMBER SYSTEMS:

What was the easiest problem for you in this section?

What was the most difficult problem for you in this section?

Which types of problems do you feel you've mastered in this section?

Which types of problems do you need to "watch out" for in this section?

EXPRESSIONS AND EQUATIONS:

What was the easiest problem for you in this section?

What was the most difficult problem for you in this section? _____

Which types of problems do you feel you've mastered in this section?

Which types of problems do you need to "watch out" for in this section?

STUDENT REFLECTION FORM (CONTINUED)

FUNCTIONS:

What was the easiest problem for you in this section?

What was the most difficult problem for you in this section? ______

Which types of problems do you feel you've mastered in this section?

Which types of problems do you need to "watch out" for in this section?

GEOMETRY:

What was the easiest problem for you in this section?

What was the most difficult problem for you in this section? ______

Which types of problems do you feel you've mastered in this section?

Which types of problems do you need to "watch out" for in this section?

STATISTICS AND PROBABILITY:

What was the easiest problem for you in this section? _____

What was the most difficult problem for you in this section?

Which types of problems do you feel you've mastered in this section?

Which types of problems do you need to "watch out" for in this section?

NUMBER SYSTEMS ANSWER KEY

1. Is the number $\frac{2}{3}$ rational or irrational? Rational

Why? It is written as a quotient of two integers.

2. Is the number $\sqrt{22}$ rational or irrational? Irrational

Why? The decimal form of this number neither terminates nor repeats.



Now that you are finished with this section, fill out the NUMBER SYSTEM section of the REFLECTION FORM.

EXPRESSIONS AND EQUATIONS ANSWER KEY

8.EE.1

1. Simplify each expression. Be sure your answers have positive exponents:

(a)
$$3a^{6} \cdot 6a^{4} =$$
 18 a^{10} (b) $\frac{20b^{12}}{5b^{3}} =$ **4** b^{9} (c) $(x^{4})^{6} =$ x^{24}
(d) Write 2 possible answers for this problem: $4^{3} \cdot 4^{-6} =$ $\frac{1}{4^{3}}$ or $\frac{1}{64}$

8.EE.2

- 2. Solve each problem involving square or cube roots:
- (a) What is the cube root of 27? 3

(b) What is the square root of 121? 11

- (c) Solve the equation: $x^2 + 3 = 67$ Solution(s): 8 and -8
- (d) A square has an area of 324 m^2 . What is the measure of one side? **18 meters**

8.EE.3, 4

3. Solve each problem involving scientific notation:

- (a) Write .0000306 in scientific notation: 3.06×10^{-5}
- (b) Write 7,900,000,000 in scientific notation: 7.9 x 10⁹
- (c) A CEO's salary is \$5,000,000 per year. A first-year teacher's salary is \$25,000. *How many times larger* is the CEO's salary? Keep your numbers in scientific notation as you set up and work out the problem. Show steps below:

$\frac{5 x \, 10^6}{2.5 x \, 10^4} = 2 \times 10^2$

The CEO's salary is **200** times larger.

(d) Is this number in scientific notation? 13×10^8 . (Yes or No.) No

How do you know? 13 is not a number falling in this range: 1≤ x < 10

If you answered "no," make the corrections: 1.3 x 10⁹

(d) Multiply: $(4.6 \times 10^8) \cdot (3.8 \times 10^6) = 1.748 \times 10^{15}$

EXPRESSIONS AND EQUATIONS ANSWER KEY

8.EE.5

4. The table shows the change in altitude of a hiker. What is the hiker's rate of change?

Minutes	Altitude (ft)		
0	0		
3	150		
4	200		
5	250		
6	300		

The hiker's rate of change is 50 ft./min .

8.EE.6

5. Draw a "slope triangle" on the graph to find the slope of the line. (Remember...slope is $\frac{rise}{run}$.)



Slope of the line = $2 \text{ or } \frac{2}{1}$

Now, try it again, but create a new slope triangle that is a different size. Do you get the same answer for the slope? ____Yes

Why did that happen? Explain:

Yes. The two slope triangles are similar. One was $\frac{2}{1}$ and the other was $\frac{4}{2}$. Their corresponding side lengths are proportional.

6. Write an equation for each line. Be sure your equation is in the form y = mx + b.



(a) Equation: <u>y = -1x + 1</u>





(b) Equation: $y = \frac{1}{3}x$





EXPRESSIONS AND EQUATIONS ANSWER KEY

8. Solve each equation. Show your steps:



Why does this system of equations have no solution? 4x + 2y cannot simultaneously be 8 and 6.

11. Determine if (-4, 6) is a solution for this system of equations:

$$y = x + 10$$
$$2x + y = -2$$

Is the ordered pair a solution? Yes.

Explain how you know:

When the x and values are each replaced with values from the ordered pair (x-values are replaced with -4 and y-values are replaced with 6), both equations are true statements.

Now that you are finished with this section, fill out the **EXPRESSIONS AND EQUATIONS** section of the **REFLECTION FORM**.

8.EE.7

ANSWER KEY

8.F.1

1. Tell whether or not each situation represents a function.

(a) Ordered Pair: (3, 5), (6, 8), (7, 5), (8, 10) Function? (Yes or no.) Yes.

Explain: Each input value has exactly one output value.



8.F.2

2. Tell which function has a greater rate of change...the graph or the table:



x	У
8	76
4	60
0	44
-4	28
-8	12

Which has the greater rate of change?

The table

ANSWER KEY

3. Graph each equation. Then tell whether or not your graph represents a function.



4. Write an equation in function form for each linear relationship below:





8.F.5





(c) Equation: y = -1x - 3

5. The graph at the right tells a story. In your own words, describe what is happening to the y-values as the x-values are increasing from 0 to 10. Be sure to use words like increase, decrease, constant, linear, or nonlinear.

When the x-values are between 0 and 3, the y-values show a linear increase from 0 to 7. When the x-values are between 3 and 6, the y-values show a nonlinear decrease from 7 to 5. When the x-values are between 6 and 7, the y-values show a linear increase from 5 to 7. When the x-values are between 7 and 10, the y-values stay constant at 7.



8.F.3



6. Sketch a graph that could exhibit the qualities in the description below:

Between the x values of 0 and 4, the y values increase in a nonlinear pattern. Then, the y values stay constant between the x values of 4 and 6. Then, from x values of 6 to 10, the y values decrease in a linear pattern.



the qualities. Answers may vary, but this general shape should be evident.

Now that you are finished with this section, fill out the **FUNCTIONS** section of the **REFLECTION FORM**.

8.F.5

GEOMETRY ANSWER KEY

8.G.1

1. Triangle ABC has coordinates A(-8, 6), B(-4, 5), C(-6, 3). Complete the series of transformations below. Graph each new image and give the new image coordinates:



Step 1: Reflect the image over the y-axis. Coordinates of the image: A'(8, 6) B'(4, 5) C'(6, 3)

Step 2: Rotate the image 180° about the origin. Coordinates of the new image: A''(-8, -6) B''(-4, -5) C''(-6, -3)

Step 3: Translate the image using the rule $(x, y) \rightarrow (x + 4, y - 1)$. Coordinates of the final image: A^{'''}(-4, -7) B^{'''}(0, -6) C^{'''}(-2, -4)

8.G.2

Question to Consider: Is the final image congruent to your preimage? Yes or No: Yes. Why?

The final image is the exact same size and shape of triangle ABC. The figure was moved; it did not change size/shape.

8.G.2

2. A line segment is moved 5 units to the left and 4 units down in the coordinate plane. Give a coordinate rule for the translation:

 $(x, y) \rightarrow (x - 5, y - 4)$

Are both line segments congruent? Yes or No: Yes.

Why? The image is the exact same size and shape of the preimage. The segment was moved; it did not change size/shape.

[8.G.3 GEOMETRY
3.	Give the rule in coordinate notation for a reflection over the x-axis: $(x, y) \rightarrow (x, -y)$
4.	Give the coordinate rule for a reflection over the y-axis: $(x, y) \rightarrow (-x, y)$
5.	Give the coordinate rule for a 180° rotation about the origin: $(x, y) \rightarrow (-x, -y)$
6.	Give the coordinate rule for a 90° clockwise rotation about the origin: $(x, y) \rightarrow (y, -x)$
7.	Give the coordinate rule for a 90° counterclockwise rotation about the origin: $(x, y) \rightarrow (-y, x)$
8.	Give the coordinate rule for a dilation of a figure using a scale factor of 3: $(x, y) \rightarrow (3x, 3y)$
W	hich type of dilation does your rule represent? (Enlargement or Reduction): Enlargement

9. A triangle is translated 8 units to the left and 2 units up in the coordinate plane. Describe the rule in coordinate notation: $(x, y) \rightarrow (x - 8, y + 2)$

8.G.4

10. Dilate triangle ABC using the rule $(x, y) \rightarrow (\frac{1}{3}x, \frac{1}{3}y)$. Be sure to label the vertices of your image.



Are $\triangle ABC$ and $\triangle A'B'C'$ similar? (Yes or No): Yes.

Why or why not?

They are both the same shape, but not the same size. Each side of the image is $\frac{1}{3}$ as long as each corresponding side of the preimage.

Are $\triangle ABC$ and $\triangle A'B'C'$ congruent? (Yes or No): **No.**

Why or why not? They are not the same size.

11. Which type of transformations will result in a congruent image? **Reflections, Rotations, Translations**

12. Explain what it means for 2 figures to be congruent: They are the same exact size and shape. GEOMETRY ANSWER KEY

13. Use the diagram below to find the missing angle measures.



14. Use the diagram below to answer the fill in the blanks. Lines a and b are parallel:





15. ΔABC and ΔDEF are similar. If $m \angle B = 62^\circ$, then $m \angle E = 62^\circ$



8.G.5

GEOMETRY ANSWER KEY

8.G.6

17. Explain how you know this is a right triangle:

If $a^2 + b^2 = c^2$, then the triangle is a right triangle.

 $8^2 + 15^2 = 17^2$ 64 + 225 = 289 8 units

8.G.7

18. A ladder is leaning against a brick wall. The bottom of the ladder is 5 feet from the wall. The top of the ladder reaches the wall 12 feet up from the ground. **How long is the ladder?**

Steps and Solution: $5^{2} + 12^{2} = c^{2}$ $25 + 144 = c^{2}$ $169 = c^{2}$ c = 13 ft



19. A 6 inch spoon is placed inside a cylinder. It is angled such that the end of the spoon handle rests 3 inches from the bottom of the cylinder. What is the diameter of the cylinder? Round your answer to the nearest hundredths place.

Steps and Solution: $a^{2} + b^{2} = c^{2}$ $3^{2} + b^{2} = 6^{2}$ $9 + b^{2} = 36$ $b^{2} = 27$



8.G.8

20. Use the Pythagorean Theorem to find the distance between points A and B in the coordinate plane. Round your answer to the nearest hundredths place.

 $b \approx 5.20$ inches

Steps and Solution:

 $3^{2} + 7^{2} = c^{2}$ 9 + 49 = c^{2} 58 = c^{2} c ≈ 7.62 units



GEOMETRY ANSWER KEY

8.G.9

21. Find the volume of the cone, cylinder and sphere below. Use 3.14 for π . Round all answers to the nearest whole number:



22. For the back-to-school open house, the middle school put a huge blow-up pencil in the front of the building! Find the volume of the pencil. Use 3.14 for π and round your final answer to the whole number.



Show Steps and Solution:

Volume of hemisphere (eraser):Volume of the cylinder: $V = \frac{1}{2} \cdot \frac{4}{3} \pi r^3$ $V = \pi r^2 h$ $V = \frac{1}{2} \cdot \frac{4}{3} (3.14)(4)^3$ $V = (3.14)(4)^2 (20)$ $V \approx 134 ft^3$ $V \approx 1,005 ft^3$

Volume of the cone (pencil tip):

V =
$$\frac{1}{3}$$
πr²h
V = $\frac{1}{3}$ (3.14) (4)²(7)
V ≈ 117 ft³

Now, add all 3 sections together: $134 + 1,005 + 117 \approx 1,256 ft^3$

Now that you are finished with this section, fill out the **GEOMETRY** section of the **REFLECTION FORM**.

STATISTICS AND PROBABILITY ANSWER KEY

8.SP.1

1. Which scatterplot below *best* illustrates the relationship between hours studying and test scores earned? *Circle your choice:*







Explain how you decided:

The more hours spent studying, the higher the test scores.

2. Create a scatterplot below that shows these characteristics: **Negative Correlation**



Answers will vary, but the graph should show a trend in this direction.



Hours Spent Exercising

What might your scatterplot depict? Give a real-world example of a situation your graph could represent:

The more hours spent exercising, the more your weight will decrease. The outlier could represent someone who has a higher muscle mass, or he/she could be increasing their food intake while exercising!

8.SP.2

3. Draw a line of fit for the scatterplot below:





5. Find 8 friends or family members and measure their height, foot length, and hair length. Fill in each table below with the data. Afterward, answer the questions at the right:

Height (cm)	Foot Length (cm)	Height (cm)	Hair Length (cm)

(a) What association(s), if any, do you see for the Height/Foot Length table?
Data will vary, but most students will notice that the taller the height, the longer the foot length (a positive correlation.)
(b) What association(s), if any, do you see for the Height/Hair Length table?
Data will vary, but most students will see no correlation between hair length and height.

Now that you are finished with this section, fill out the **STATISTICS AND PROBABILITY** section of the **REFLECTION FORM**.